



Review of some mathematical tools:

- Linear systems of differential equations
- Non-linear systems of differential equations
 - phase portrait
 - critical (or, equilibrium) points



- A linear system of ODEs has form

$$\mathbf{y}' = \mathbf{A}\mathbf{y} + \mathbf{p}$$

- Initial condition $\mathbf{y}(t=0) = \mathbf{y}_0$
- The solution can be written using the matrix exponential

$$\mathbf{y}(t) = e^{\mathbf{A}t} \mathbf{y}_0 + \int_0^t e^{\mathbf{A}(t-s)} \mathbf{p}(s) ds$$



- Of particular interest are states of the system for which $\mathbf{y}' = 0$, known as critical or equilibrium points, obtained by solving a linear system

$$\mathbf{A}\mathbf{y} + \mathbf{p} = 0 \Rightarrow \mathbf{A}\mathbf{y} = -\mathbf{p}$$